Printed Pages: 02

 Paper Id:
 1
 9
 2
 2
 3

Time: 3 Hours

Sub Code: RAS203
Roll No.

B. TECH (SEM-II) THEORY EXAMINATION 2017-18 ENGINEERING MATHEMATICS - II

Total Marks: 70

Note: Attempt all Sections. If require any missing data, then choose suitably.

SECTION A

1. Attempt all questions in brief.

- (a) Determine the differential equation whose set of independent solutions is $\{e^x, xe^x, x^2e^x\}$.
- **(b)** Solve: $(D+1)^3 y = 2e^{-x}$.
- (c) Prove that: $P_n(-x) = (-1)^n P_n(x)$.
- (d) Find inverse Laplace transform of $\frac{s+8}{s^2+4s+5}$.
- (e) If $L\{F(\sqrt{t})\} = \frac{e^{-1/s}}{s}$, find $L\{e^{-t}F(3\sqrt{t})\}$.

(f) Solve:
$$(D+4D'+5)^2 z = 0$$
, where $D \equiv \frac{\partial}{\partial x}$, $D' \equiv \frac{\partial}{\partial y}$.

(g) Classify the equation: $z_{xx} + 2x z_{xy} + (1 - y^2) z_{yy} = 0$.

SECTION B

2. Attempt any *three* of the following:

(a) Solve $(D^2 - 2D + 4)y = e^x \cos x + \sin x \cos 3x$.

(b) Prove that:
$$J_{5/2}(x) = \sqrt{\frac{2}{\pi x}} \left[\left(\frac{3 - x^2}{x^2} \right) \sin x - \frac{3 \cos x}{x} \right].$$

(c) Draw the graph and find the Laplace transform of the triangular wave function of period 2π given by

$$F(t) = \begin{cases} t, & 0 < t \le \pi \\ 2\pi - t, & \pi < t < 2\pi \end{cases}$$

Obtain half range cosine series for e^x the function $f(t) = \begin{cases} 2t, & 0 < t < 1 \\ 2(2-t), 1 < t < 2 \end{cases}$

(e) Solve by method of separation of variables:
$$\frac{\partial u}{\partial t} = \frac{\partial u}{\partial x} - 2u$$
; $u(x,0) = 10e^{-x} - 6e^{-4x}$

SECTION C

3. Attempt any one part of the following:

(a) Solve the simultaneous differential equations:

$$\frac{d^2x}{dt^2} - 4\frac{dx}{dt} + 4x = y \text{ and } \frac{d^2y}{dt^2} + 4\frac{dy}{dt} + 4y = 25x + 16e^t.$$

(b) Use variation of parameter method to solve the differential equation $x^2y'' + xy' - y = x^2e^x$.

$7 \times 3 = 21$

$2 \ge 7 = 14$

 $7 \times 1 = 7$

4. Attempt any one part of the following:

- (a) State and prove Rodrigue's formula for Legendre's polynomial.
- Solve in series: 2x(1-x)y'' + (1-x)y' + 3y = 0. (b)

Attempt any one part of the following: 5.

State convolution theorem and hence find inverse Laplace transform of $\frac{s^2}{(s^2 + a^2)(s^2 + b^2)}$. **(a)**

Solve the following differential equation using Laplace transform $\frac{d^3 y}{dt^3} - 3\frac{d^2 y}{dt^2} + 3\frac{dy}{dt} - y = t^2 e^t$ (b) where y(0) = 1, y'(0) = 0 and y''(0) = -2.

6. Attempt any one part of the following:

 $f(x) = \begin{cases} x, & -\pi < x \le 0 \\ -x, & 0 < x < \pi \end{cases}$ and hence show that Obtain Fourier series for the function **(a)**

$$\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}$$

Solve the linear partial differential equation: $\frac{\partial^2 z}{\partial x^2} - 2 \frac{\partial^2 z}{\partial x \partial y} = \sin x \cos 2y$. **(b)**

7. Attempt any one part of the following: **(a)**

- A string is stretched and fastened to two points l apart. Motion is started by displacing the string in the form $y = A \sin \frac{\pi x}{l}$ from which it is released at time t = 0. Find the displacement of any point at a distance x from one end at any time t.
- **(b)** A rectangular plate with insulated surfaces is 8 cm wide and so long compared to its width that it may be considered infinite in length without introducing an appreciable error. If the temperature

along one short edge y = 0 is given by $u(x,0) = 100\sin\frac{\pi x}{9}, 0 < x < 8$

while the two long edges x = 0 and x = 8 as well as the other short edge are kept at $0^{\circ}C$. Find the temperature u(x, y) at any point in steady state.

 $7 \times 1 = 7$

 $7 \ge 1 = 7$

 $7 \times 1 = 7$

 $7 \times 1 = 7$