

1 Answer any four parts of the following :

5×4=20

- (a) Define unit step, unit impulse and unit ramp using mathematical expressions.
- (b) The waveform is shown in Fig. 1(b). Write an equation for this waveform v(t) using step functions :



Fig. 1(b)

(c) Compare the mechanical system with electrical system using force-voltage analogy. Also write suitable expressions of it.

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[Contd...

- (d) Distinguish between time invariant and time varying system with suitable example.
- (e) Consider a series R-L circuit shown in Fig. 1(e). The switch is used at time t = 0. Find current i(t) using classical method.



Fig. 1(e)



What is sinusoidal function ? Explain, why alternating voltage (current) of sinusoidal form is used in system analysis.

2 Attempt any two parts of the following :

(a) Find the trigonometric Fourier series for continuous time saw-tooth wave shown in Fig. 2(a).



- (b) Define odd and even function in Fourier analysis. Also find the Fourier coefficients of rectified sine wave form.
- (c) Explain the Fourier symmetry. Write the Fourier transform of step, ramp and impulse signals for system analysis.

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[Contd...

 $10 \times 2 = 20$

Attempt any two parts of the following :

(a) Find $L[t^2 \sin wt]$ using the relation

$$L[t f(t)] = -\frac{d}{ds}f(s).$$

(b)

3

1

4

Using Laplace transform solve differential equation

$$2\frac{d^2x}{dt^2} + 7\frac{dx}{dt} + 6x = 0$$

with
$$x(0) = 0$$
, $\frac{dx}{dt} = 1$.

(c) Explain initial value and final value theorems in Laplace analysis. Also find the

final value of
$$F(s) = \frac{2s}{(s+2)(s+5)}$$
.

Attempt any two parts of the following :

(a) In the network shown in Fig. 4(a), formulate and find the solution for $i_1(t)$ and $i_2(t)$ using state equations.



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Assume zero initial conditions.

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[Contd...

 $10 \times 2 = 20$

$$\frac{d^{3}y}{dt^{3}} + 3\frac{d^{2}y}{dt^{2}} + 4\frac{dy}{dt} + y = \frac{d^{3}u}{dt^{3}} + 3\frac{d^{2}u}{dt^{2}} + \frac{du}{dt} + 2u(t)$$

in its standard state space form.

- (c) State and explain controllability and observability in state-space analysis. Enlist the condition for controllability and observability of a system.
- Attempt any two parts of the following :

 $10 \times 2 = 20$

(a) Find z-transform of the following :

(i) $x(n) = a^n u(n)$

- (ii) $x(n) = -b^n u(n-1)$
- (b) Explain the public transfer function approach used in Z-transform analysis with the help of suitable example.
- (c) Using Z-transform analysis, solve differential equation

 $\ddot{x} + 4\dot{x} + 8x = 0$

with x(0) = 3 and $\overline{x}(0) = -4$.

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1.0

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