Roll No: $\square$

## B. TECH <br> (SEM-III) THEORY EXAMINATION 2019-20 <br> MATHEMATICS-IV

Time: 3 Hours
Total Marks: 100
Note: 1. Attempt all Sections. If require any missing data; then choose suitably.

## SECTION A

## 1. Attempt all questions in brief.

$2 \times 10=20$

| Q no. | Question | Marks | CO |
| :---: | :---: | :---: | :---: |
| a. | Solve the following partial differential equation $y q-x p=z$. | 2 | 1 |
| b. | Solve the Cauchy's problem $u_{x}-u_{y}=0 . u(x, 0)=x$ | 2 | 1 |
| c. | Classify the following equation. $x^{2} \frac{\partial^{2} u}{\partial t^{2}}-\frac{\partial^{2} u}{\partial t^{2}}=u$ | 2 | 2 |
| d. | Solve the partial differential equation $\frac{\partial^{2} z}{\partial x^{2}}+\frac{\partial^{2} z}{\partial x \partial y}=0$. | 2 | 2 |
| e. | Find the median of $6,8,9,10,11,12.13$. | 2 | 3 |
| f. | The first three central moments of a distribution are $0,15,-31$. Find the moment of coefficient of skewness. | 2 | 3 |
| g . | If the p.m.f of a discrete random variable X is <br> Determine $E(X)$ and $V(X)$. | $2$ | 4 |
| h. | The probability density function $f(x)$ of a continuous random variable X is defined by $\mathrm{f}(\mathrm{x})= \begin{cases}\frac{A}{x^{2}}, & 5 \leq \mathrm{x} \leq 10 \\ 0, & \text { otherwise }\end{cases}$ Find the value of A. | 2 | 4 |
| i. | Find the mean of the Binomial Distribution $\mathrm{B}\left(4, \frac{1}{3}\right)$. | 2 | 4 |
| j. | A machine which produces mica insulating washers for use in electric device to turn out washers having a thickness of 10 mm . A sample of 10 washers hasan average thickness 9.52 mm with a standard deviation of 0.6 mm . Find out t . | 2 | 5 |

## SECTION B

## 2. Attempt any three of the following:

$\mathbf{3 \times 1 0}=\mathbf{3 0}$

| Q no. | Question | Marks | CO |
| :--- | :--- | :--- | :--- |
| a. | Solve $\left(D^{2}-D D^{\prime}-2 D^{\prime 2}\right) z=(y-1) e^{x}$ | 10 | 1 |
| b. | A rectangular plate with insulated surface is 10 cm wide and so long compared to its <br> width that it may be considered infinite in length without introducing an appreciable <br> error. If the temperature along the short edge $\mathrm{y}=0$ is given by: <br> $\mathrm{u}(\mathrm{x}, 0)==$$20 \mathrm{x} 0 \leq \mathrm{x} \leq 5$ <br> $20(10-\mathrm{x}) 5<\mathrm{x}<10$ <br> While the two edges $\mathrm{x}=0$ and $\mathrm{x}=10$ as well as the other short edge are kept at $0^{\circ} \mathrm{C}$. <br> Find the steady state temperature at any point $(\mathrm{x}, \mathrm{y})$ of the plate. | 2 |  |

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## 3. Attempt any one part of the following:

$1 \times 10=10$

| Q no. | Question | Marks | CO |
| :--- | :--- | :--- | :--- |
| a. | Solve $(D+1)\left(D+D^{\prime}-1\right) z=\sin (2 x+3 y)$ | 10 | 1 |
| b. | In a partial destroyed laboratory record of an analysis of correlation data, the following result <br> only are legible : <br> Variance of $\mathrm{x}=9$ | 10 | 3 |
| Regression equation: $8 \mathrm{x}-10 \mathrm{y}+66=0,40 \mathrm{x}-18 \mathrm{y}=214$. <br> What were (a) the mean value of x and y (b) the standard deviation of y and the co-efficient of <br> correlation between x and y ? |  |  |  |

## 4. Attempt any one part of the following:

$1 \times 10=10$

| Q no. | Question | Marks | CO |
| :--- | :--- | :--- | :--- |
| a. | Solve $x^{2} \frac{\partial^{2} z}{\partial x^{2}}-4 y^{2} \frac{\partial^{2} z}{\partial y^{2}}-4 y \frac{\partial z}{\partial y}-z=x^{2} y^{2} \log y$ |  |  |$) 10$| 1 |
| :--- |
| b. |
| A tightly stretched string with fixed end points $\mathrm{x}=0$ and $x=l$ is initially in a <br> position given by $y=y_{0} \sin ^{3} \frac{\pi x}{l}$. If it is released from rest from this position, find <br> the displacement $\mathrm{y}(\mathrm{x}, \mathrm{t})$. |

## 5. Attempt any one part of the following:

$1 \times 10=10$

| Q no. | Question | Marks | CO |
| :--- | :--- | :--- | :--- |
| a. | An insulated rod of length $l$ itsends A and B maintained at $0^{\circ} \mathrm{C}$ and $100^{\circ} \mathrm{C}$ <br> respectively until the steady state condition prevails. If B is suddenly reduced to $0^{\circ} \mathrm{C}$ <br> and maintained at $0^{\circ} \mathrm{C}$, Find the temperature at a distance x from A at time t. | 2 |  |

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| b. | Find the multiple regression equation of $\mathrm{X}_{1}$ on $\mathrm{X}_{2}$ and $\mathrm{X}_{3}$ from the data          <br> Given below:          <br> $\mathrm{X}_{1}$ 3 5 6 8 12 10 <br> $\mathrm{X}_{2}$ 10 10 5 7 5 2 <br> $\mathrm{X}_{3}$ 20 25 15 16 15 2          <br>        10   |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

6. Attempt any one part of the following:
$1 \times 10=10$

| Q no. | Question | Marks | CO |
| :--- | :--- | :--- | :--- |
| a. | State the Bayes' theorem. The probability that a civilian can hit a target is $\frac{2}{5}$ and the <br> probability that an army officer can hit the same target is $\frac{3}{5}$ While the civilian canfire <br> 8 shots in the time, the army officer fires 10 shots. If they fire together, then what is <br> the probability that army officer shoots the target? | 10 | 4 |
| b. | Define the Normal distribution. The daily wages of 1000 workers are distributed <br> around a mean of Rs. 140 and with a standard deviation of Rs. 10. Estimate the <br> number of workers whose daily waged will be (i) between Rs. 140 and Rs. 144, (ii) <br> less than Rs. 126 (iii) more than Rs. 160. | 10 | 4 |

7. Attempt any one part of the following:

$$
1 \times 10=10
$$



