## **B. TECH** (SEM-III) THEORY EXAMINATION 2019-20 **MATHEMATICS-IV**

# Time: 3 Hours

Note: 1. Attempt all Sections. If require any missing data; then choose suitably.

Roll No:

## **SECTION A**

#### Attempt all questions in brief. 1.

Q no.	Question	Marks	CO
a.	Solve the following partial differential equation $yq - xp = z$ .	2	1
b.	Solve the Cauchy's problem $u_x - u_y = 0$ . $u(x, 0) = x$	2	1
с.	Classify the following equation. $x^2 \frac{\partial^2 u}{\partial t^2} - \frac{\partial^2 u}{\partial t^2} = u$	2	2
d.	Solve the partial differential equation $\frac{\partial^2 z}{\partial x^2} + \frac{\partial^2 z}{\partial x \partial y} = 0.$	2	2
e.	Find the median of 6,8,9,10,11,12.13.	2	3
f.	The first three central moments of a distribution are 0,15,-31. Find the moment of coefficient of skewness.	2	3
g.	If the p.m.f of a discrete random variable X is	2	4
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	00.	$O_{2}$
h	The probability density function $f(x)$ of a continuous random variable	2	Δ
11.	X is defined by $f(x) = \begin{bmatrix} \frac{A}{x^2}, & 5 \le x \le 10 \\ 0, & \text{otherwise} \end{bmatrix}$ Find the value of A.	2	*
i.	Find the mean of the Binomial Distribution $B(4, \frac{1}{3})$ .	2	4
j.	A machine which produces mica insulating washers for use in electric device to turn out washers having a thickness of 10 mm. A sample of 10 washers hasan average thickness 9.52 mm with a standard deviation of 0.6 mm. Find out t.	2	5

# SECTION B

#### Attempt any *three* of the following: 2.

3	X	1	0	=	3(	)
3	X	1	U	=	3(	J

Q no.	Question	Marks	CO
a.	Solve $(D^2 - DD' - 2D'^2)z = (y - 1)e^x$	10	1
b.	A rectangular plate with insulated surface is 10 cm wide and so long compared to its	10	2
	width that it may be considered infinite in length without introducing an appreciable		
	error. If the temperature along the short edge y=0 is given by:		
	$\mathbf{u}(\mathbf{x},0) = 20\mathbf{x} \ 0 \leq \mathbf{x} \leq 5$		
	20 (10-x) 5 <x<10< th=""><th></th><th></th></x<10<>		
	While the two edges $x=0$ and $x=10$ as well as the other short edge are kept at 0°C.		
	Find the steady state temperature at any point $(x,y)$ of the plate.		

# $2 \ge 10 = 20$

Total Marks: 100

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Paper 3	Id: 199352	Rol	ll No:			
с.	Find an exponentV501P1354	ial curve $PV^{\gamma} = k$ 100 150 200 48 26 17	t for the data:		10 3	
d.	Fit a Poisson distributionper square for 400X01F10314It is given that $e^{-1}$	ribution to the foll ) squares	lowing data whic567420	h give the number of yeast cells $8$ $9$ $10$ $0$ $0$	10 4	
e.	To test the effect obtained Inoculated Not inoculated Total (The figure represent Use Chi square attack from chole	Attached30140170sents the number of test to defend orra. The value of $\chi$	lation against che Not attached 160 460 620 of persons) refute the states <sup>2</sup> for 1 degree of	olera , the following table was   Total   190   600   790   ment. The inoculation prevents   freedom at 5% level is 3.841.	10 5	

#### Attempt any one part of the following: 3.

3.	Attempt any <i>one</i> part of the following: $1 \times 10 = 10$	0	2
Q no.	Question	Marks	CO
a.	Solve $(D + 1)(D + D' - 1)z = \sin(2x + 3y)$	10	1
b.	In a partial destroyed laboratory record of an analysis of correlation data, the following result only are legible : Variance of $x = 9$ Regression equation: $8x-10y + 66 = 0$ , $40x - 18y = 214$ . What were (a) the mean value of x and y (b) the standard deviation of y and the co-efficient of correlation between x and y?	10	3

#### Attempt any one part of the following: 4.

# $1 \ge 10 = 10$

Q no.	Question	Marks	CO
a.	Solve $x^2 \frac{\partial^2 z}{\partial x^2} - 4y^2 \frac{\partial^2 z}{\partial y^2} - 4y \frac{\partial z}{\partial y} - z = x^2 y^2 \log y$	10	1
b.	A tightly stretched string with fixed end points x=0 and $x = l$ is initially in a position given by $y = y_0 sin^3 \frac{\pi x}{l}$ . If it is released from rest from this position, find the displacement y(x,t).	10	2

#### Attempt any one part of the following: 5.

### $1 \ge 10 = 10$

Q no.	Question	Marks	CO
a.	An insulated rod of length $l$ itsends A and B maintained at 0°C and 100° C	10	2
	respectively until the steady state condition prevails. If B is suddenly reduced to 0°C		
	and maintained at 0°C, Find the temperature at a distance x from A at time t.		

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b.	Find the	e multiple	regression	equation	of $X_1$ on $Z$	$X_2$ and $X_3$	from the data
	Given b	pelow:					
	$X_1$	3	5	6	8	12	10
	X2	10	10	5	7	5	2
	X3	20	25	15	16	15	2

Roll No:

#### Attempt any one part of the following: 6.

# $1 \ge 10 = 10$

10

3

Q no.	Question	Marks	CO
a.	State the Bayes' theorem. The probability that a civilian can hit a target is $\frac{2}{5}$ and the	10	4
	probability that an army officer can hit the same target is $\frac{3}{5}$ While the civilian canfire		
	8 shots in the time, the army officer fires 10 shots. If they fire together, then what is		
	the probability that army officer shoots the target?		
b.	Define the Normal distribution. The daily wages of 1000 workers are distributed	10	4
	around a mean of Rs. 140 and with a standard deviation of Rs. 10. Estimate the		
	number of workers whose daily waged will be (i) between Rs. 140 and Rs. 144, (ii)		
	less than Rs. 126 (iii) more than Rs. 160.		

#### 7. Attempt any *one* part of the following:

# $1 \ge 10 = 10$

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7.	Attempt any one part of the following: $1 \times 10 = 10$
Q no.	Question Marks CO
a.	An IT company wants to appoint an effective trainer to improve the performance of their engineers. Four group of 7,8,10 and 11 engineers from total 36 engineers were given 5 days training by the 4 trainers. Scores were awarded to the engineers at the end of the training on their Skills. Let us examine the preference of one engineer of one trainer over other three trainers. Given that $\alpha$ =0.05 i.e at 5% level of significance the value of F (3,32)=3.29.
b.	Distinguish between p chart and C chart. The number of defectives in 17 samples of size 500 each from 17 lots is shown below:105 $\boxed{\text{Samp 1}}$ 23456789101111314151617
	No.of defec tives 20 25 35 45 15 65 15 20 35 23 12 9 21 22 32 35 38   Find out the control limits for the number of defective units and also check whether the process is under control or not. Image: Control or not is and also check whether Image: Control or not is and also check whether
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