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## BTECH

(SEM III) THEORY EXAMINATION 2021-22

Time: 3 Hours
Total Marks: 100
Note: Attempt all Sections. If require any missing data; then choose suitably.

## SECTION A

1. Attempt all questions in brief. $2 \times 10=20$

| a. | What do you mean by energy and power signals? |
| :--- | :--- |
| b. | Explain conjugate symmetry and conjugate asymmetry. |
| c. | What do you mean by auto and cross correlation functions? |
| d. | Show that the product of two even signals or of two odd signals is an even signal and that the <br> product of an even and an odd signal is an odd signal. |
| e. | Consider the discrete time signal $\boldsymbol{x}[\boldsymbol{n}]=\mathbf{1}-\sum_{\boldsymbol{k}=\boldsymbol{3}}^{\infty} \boldsymbol{\delta}[\boldsymbol{n}-\mathbf{1}-\boldsymbol{k}]$. Determine the values of <br> integers $\mathbf{M}$ and $\mathbf{n}_{\boldsymbol{0}}$ so that $\boldsymbol{x}[\boldsymbol{n}]$ may be expressed as $\boldsymbol{x}[\boldsymbol{n}]=\boldsymbol{u}\left[\mathbf{M n}-\boldsymbol{n}_{\boldsymbol{o}}\right]$. |
| f. | What do you mean by region of convergence? |
| g. | Define auto co-relation function. |
| h. | What do you mean by Eigen signal and Eigen value? |
| i. | What do you mean by over damped, under damped and critically camped system? |
| j. | Define rise time and band width of a second order continuous time system. |

## SECTION B

2. Attempt any three of the following:

| a. | If $\boldsymbol{X}(\boldsymbol{s})=\frac{2 S+3}{(S+1)(S+2)}$. Find $\boldsymbol{x}(\boldsymbol{t})$ for <br> i. System is stable <br> ii. System is causal <br> iii. System is stable and causal. |
| :---: | :---: |
| b. | Determine whether the following signal is periodic? If periodic then determine the period: <br> i. $\quad x(t)=2 \sin \left(\frac{2}{3}\right) t+3 \cos \left(\frac{2 \pi}{5}\right) t$ <br> ii. $\quad x(t)=3 \sin t+3 \cos \left(\frac{4}{3}\right) t$ <br> iii. $\quad x(n)=\cos \left(\frac{\pi n}{7}\right) \sin \left(\frac{\pi n}{7}\right)$ <br> iv. $\quad x(n)=e^{j \frac{\pi n}{16}} \cos \left(\frac{\pi n}{17}\right)$ |
| c. | If input $\mathrm{x}[\mathrm{n}]$ and output $\mathrm{y}[\mathrm{n}]$ are related by $\boldsymbol{y}[\boldsymbol{n}]=\boldsymbol{x}[\boldsymbol{n}]\{\boldsymbol{g}[\boldsymbol{n}]+\boldsymbol{g}[\boldsymbol{n}-\mathbf{1}]\}$ <br> i. If $\mathbf{g}[\mathbf{n}]=\mathbf{1} \forall \mathbf{n}$, show that this system is time invariant. <br> ii. If $\mathbf{g}[\mathbf{n}]=\mathbf{n} \forall \mathbf{n}$, show that this system is time variant. <br> iii. If $\mathbf{g}[\mathbf{n}]=\mathbf{1}+\left[-\mathbf{1}^{\mathbf{n}}\right] \forall \mathbf{n}$, show that this system is time invariant. |
| d. | Find the inverse Z transform of the following for all possible cases of ROC. $X(Z)=\frac{(Z+2)}{2 Z^{2}-7 Z+3}$ |

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e. $\quad$ Find the continuous time Fourier transform of the Gate /Rectangular signal. Also plot its magnitude response.

## SECTION C

3. Attempt any one part of the following:
$10 \times 1=10$

| a. | Using Fourier transform, find the convolution of following signals <br> $\boldsymbol{x}_{\mathbf{1}}(\boldsymbol{t})=\boldsymbol{e}^{-\mathbf{2 t}} \boldsymbol{u}(\boldsymbol{t})$ <br> $\boldsymbol{x}_{\mathbf{2}}(\boldsymbol{t})=\boldsymbol{e}^{-\mathbf{3 t}} \boldsymbol{u}(\boldsymbol{t})$ |
| :---: | :--- |
| b. | Find the convolution of two rectangular pulses of amplitudes A and duration T. Also plot the <br> result with time. |

4. Attempt any one part of the following:

| a. | Define the systems with the following characteristics: <br> i. Static or Dynamic <br> ii. Linear or Non-Linear <br> iii. Causal or Non-Causal <br> iv. Time variant or In-variant |
| :---: | :---: |
| b. | Calculate the DTFT of the following using properties of DTFT. <br> i. $\quad \boldsymbol{x}(n)=\boldsymbol{u}(n+3)-\boldsymbol{u}(n-3)$ <br> ii. $\quad \boldsymbol{x}(\mathrm{n})=\boldsymbol{u}(\boldsymbol{n})$ |
| 5. | Attempt any one part of the following: $10 \times 1=10$ |
| a. | Solve the difference equation using $Z$ transform method: $x(n-2)-9 x(n-1)+18 x(n)=0$ <br> Initial conditions are $x(-1)=1, x(-2)=9$. |
| b. | Determine whether the following signal is energy or power signal. $x(n)=u[n]-u[n-6]$ |
| 6. | Attempt any one part of the following: 10x1=10 |


| a. | A continuous time system is described by differential equation $y^{\prime \prime}(\boldsymbol{t})+3 \boldsymbol{y}^{\prime}(\boldsymbol{t})+2 \boldsymbol{y}(\boldsymbol{t})=$ <br> $\boldsymbol{x}(\boldsymbol{t})$. Find the impulse response of the system. If the input is $\boldsymbol{x}(\boldsymbol{t})=4 \boldsymbol{e}^{-2 \boldsymbol{t}} \boldsymbol{u}(\boldsymbol{t})$, determine <br> the system output corresponding to this input. |
| :---: | :--- |
| b. | Analyze the first order continuous time low pass filter with its pole zero location and <br> response. |

7. Attempt any one part of the following:

| a. | State and prove the various properties of Laplace Transform. |  |
| :---: | :--- | :--- |
| b. | Prove the following properties of Z transform: |  |
|  | i. | Linearity |
|  | ii. | Time invariance |
|  | iii. | Parseval's relation |
| iv. | Convolution |  |

