## Roll No:



BTECH
(SEM III) THEORY EXAMINATION 2021-22

## MATHEMATICS-III

Time: 3 Hours
Total Marks: 100
Notes:

- Attempt all Sections and Assume any missing data.
- Appropriate marks areallotted to each question, answer accordingly.

| SECTION-A Attempt All of the following Questions in brief | Marks(10X2=20) | CO |
| :--- | :--- | :---: |
| Q1(a) | Find the Laplace transform of $\int_{0}^{t} e^{-t}$ cost $d t$. | 1 |
| Q1(b) | Evaluate: $L^{-1}\left(\frac{e^{-2 p}}{p^{2}}\right)$. | 1 |
| Q1(c) | State Modulation theorem. | 2 |
| Q1(d) | Find the Z-transform of $f(k)=\frac{1}{k}, k \geq 1$. | 2 |
| Q1(e) | Prove that the statement $(p \rightarrow q) \rightarrow(p \wedge q)$ is a contingency. | 3 |
| Q1(f) | Show that every sub- group H of an abelian group G is normal. | 3 |
| Q1(g) | How many bit strings of length 8 either start with 1 or end with two bits $00 ?$ | 4 |
| Q1(h) | Given $f(x)=3 x-2$, find $f-1(x)$. | 4 |
| Q1(i) | Define Maximal element and Minimal element of Poset. | 5 |
| Q1(j) | Prove the Boundedness $($ NULL $)$ law i.e. $a * 0=0$. | 5 |



| SECTION-C Attempt ANY ONE following Question Marks $(\mathbf{1 X 1 0}=\mathbf{1 0})$ | CO |  |
| :--- | :--- | :---: | :---: |
| Q3(a) | Draw the graph and find the Laplace transform of the triangular wave function of |  |
|  | period of 2c given by $f(t)=\left\{\begin{array}{cl}t, & 0<t \leq c \\ 2 c-t \quad c<t<2 c\end{array}\right.$ | 1 |
| Q3(b) | Prove that: $\quad L^{-1}\left\{\frac{1}{\left(p^{2}+1\right)^{3}}\right\}=\frac{1}{8}\left[\left(3-t^{2}\right) \sin t-3 t \operatorname{cost}\right]$ | 1 |


| SECTION-C Attempt ANY ONE following Question Marks (1X10=10) | CO |  |
| :--- | :--- | :---: |
| Q4(a) | Determine the distribution of temperature in the semi- infinite medium $x \geq 0$ when <br> the end $x=0$ is maintained at zero temperature and the initial distribution of <br> temperature is F(x). | 2 |
| Q4(b) | Solve by Z-transform the difference equation $y_{k+2}+6 y_{k+1}+9 y_{k}=2^{k} ;$ <br> $y_{0}=y_{1}=0$. | 2 |

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| SECTION-C Attempt ANY ONE following Question Marks (1X10=10) | CO |  |
| :--- | :--- | :---: |
| Q5(a) | Consider the following argument and determine whether it is valid. <br> Either I will get good marks or I will not graduate. If I did not graduate I will go to <br> Canada. I get good marks. Thus, I would not go to Canada. | 3 |
| Q5(b) | Translate the following into symbolic form and test the validity of the argument. <br> If 6 is even then 2 does not divide 7. Either 5 is not prime or 2 divides 7. But 5 is <br> prime, therefore , 6 is odd. | 3 |


| SECTION-C Attempt ANY ONE following Question Marks (1X10=10) | CO |  |
| :--- | :--- | :---: |
| Q6(a) | Among the first 1000 positive integers: <br> (a) Determine the integers which are not divisible by 5, nor by 7, nor by 9. <br> (b) Determine the integers divisible by 5, but not by 7, not by 9. | 4 |
| Q6(b) | Prove by Mathematical Induction $\frac{1}{1 \cdot 3}+\frac{1}{3 \cdot 5}+\frac{1}{5.7}+\cdots \ldots .+\frac{1}{(2 n-1) .(2 n+1)}=\frac{n}{2 n+1}$. | 4 |


| SECTI |  | Attempt ANY ONE following Question | (1X10 | CO |
| :---: | :---: | :---: | :---: | :---: |
| Q7(a) | If $L$ be any Lattice, then for any $a, b, c \in L$. Prove the following: <br> (i) $\quad a \vee a=a$. (ii) $a \vee b=b \vee a($ iii $) a \vee(b \vee c)=(a \vee b) \vee c$ (iv) $a \vee(a \wedge b)=a$. |  |  |  |
| Q7(b) | For two posets A and B: <br> (i) Show that if $f: A \rightarrow B$ is an order preserving, then $f$ is one to one. <br> (ii) Show that if $f: A \rightarrow B$ is an order isomorphism, then there is an order isomorphism $g: B \rightarrow A$. |  |  |  |

