## BTECH

# (SEM III) THEORY EXAMINATION 2021-22 MECHANICS OF SOLIDS 

## Time: 3 Hours

Total Marks: 70
Note: 1. Attempt all Sections. If require any missing data; then choose suitably.

## SECTION A

1. Attempt all questions in brief.
$2 \times 7=14$

| a. | Explain the terms section modulus and write the expression for the same. |
| :--- | :--- |
| b. | Explain Hook's Law in brief. |
| c. | Analytically differentiate between bending of straight and curved beam. |
| d. | Define shear stresses in beam and its importance. |
| e. | Explain slenderness ratio and its relation with stress |
| f. | Differentiate between strain energy and shear strain energy. |
| g. | What are the various stresses acting on closed and open coiled springs? |

## SECTION B

2. Attempt any three of the following:

| a. | Derive the equation for principal stresses and principal planes for an element <br> subjected to compound stresses. |
| :--- | :--- |
| b. | A closely-coiled helical spring of round steel wire 5 mm in diameter having 12 <br> complete coils of 50 mm mean diameter is subjected to an axial load of 100 N. <br> Find the deflection of the spring and the maximum shearing stress in the <br> material. Modulus of rigidity (C) $=80 \mathrm{GPa}$ |
| c. | A cylindrical shell of 500 mm diameter is required to withstand an internal <br> pressure of 4 MPa. Find the minimum thickness of the shell, if maximum <br> tensile strength in the plate material is 400 MPa and efficiency of the joints is <br> $65 \%$. Take factor of safety as 5 |
| d. | A cantilever beam is rectangular in section having 80 mm width and 120 mm <br> depth. If the cantilever is subjected to a point load of 6 kN at the free end and <br> the bending stress is not to exceed 40 MPa, find the span of the cantilever beam. |
| e. | Derive the differential equation of deflection curve. |

## SECTION C

3. Attempt any one part of the following: $7 \times 1=7$
(a) In an elastic material, the direct stresses of $120 \mathrm{MN} / \mathrm{m}^{2}$ and $90 \mathrm{MN} / \mathrm{m}^{2}$ are applied at a certain point on planes at right angles to each other in tension and compressive respectively. Estimate the shear stress to which material could be subjected, if the maximum principal stress is $150 \mathrm{MN} / \mathrm{m}^{2}$. Also find the magnitude of other principal stress and its inclination to $120 \mathrm{MN} / \mathrm{m}^{2}$.
(b) The state of stress at a point in a loaded component principal stresses is found to be as given below: $\sigma_{\mathrm{x}}=50 \mathrm{GN} / \mathrm{m}^{2} ; \sigma_{\mathrm{y}}=150 \mathrm{GN} / \mathrm{m}^{2} ; \tau_{\mathrm{xy}}=100 \mathrm{GN} / \mathrm{m}^{2}$; Determine the principal stresses and maximum shearing stress. Find the orientations of the planes on which they act.
4. Attempt any one part of the following:
$7 \times 1=7$
(a) A solid circular shaft transmits 75 kW power at 200 rpm . Calculate the shaft diameter, if the twist in the shaft is not to exceed $1^{\circ}$ in 2 m length and the shear strength is limited to $50 \mathrm{MN} / \mathrm{m}^{2}$. Take $\mathrm{G}=100 \mathrm{GN} / \mathrm{m}^{2}$.

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(b)

A steel bar 10 cm wide and 8 mm thick is subjected to bending moment. The radius of neutral surface is 100 cm . Determine maximum and minimum bending stress in the beam.
5. Attempt any one part of the following: $7 \times 1=7$

| (a) | An open coil helical spring made up of 10 mm diameter wire and of mean <br> diameter of 100 mm has 12 coils, angle of helix being $15^{\circ}$. Determine the axial <br> deflection and the intensities of bending and shear stresses under an axial load <br> of 500 N. Take C as 80 GPa and E as 200 GPa |
| :--- | :--- |
| (b) | An I section joist $400 \mathrm{~mm} \times 200 \mathrm{~mm} \times 20 \mathrm{~mm}$ and 6 m long is used as a strut <br> with both ends fixed. What is Euler's crippling load for the column? Take <br> Young's modulus for the joist as 200 GPa |

6. Attempt any one part of the following:
(a) A cylindrical vessel 2 m long and 500 mm in diameter with 10 mm thick plates is subjected to an internal pressure of 3 MPa . Calculate the change in volume of the vessel. Take $\mathrm{E}=200 \mathrm{GPa}$ and Poisson's ratio $=0.3$ for the vessel material.
(b) A thick metallic cylindrical shell of 150 mm internal diameter is required to withstand an internal pressure of $8 \mathrm{~N} / \mathrm{mm}^{2}$. Find the necessary thickness of the shell, if the permissible tensile stress in the section is $20 \mathrm{~N} / \mathrm{mm}^{2}$
7. Attempt any one part of the following:
(a) A steel bar 50 mm in diameter, is formed into a circular arc of 4 m radius and supports an angle of 900 . A couple is applied at each end of the bar, which changes the slope to 950 at one end relative to the other. Calculate the maximum bending stress due to the couple. Take E as 200 GPa
(b) Two wooden planks $150 \mathrm{~mm} \times 50 \mathrm{~mm}$ each are connected to form a T-section of a beam. If a moment of $6.4 \mathrm{kN}-\mathrm{m}$ is applied around the horizontal neutral axis, inducing tension below the neutral axis, find the bending stresses at both the extreme fibres of the cross- section
