

**B.TECH.**

**THEORY EXAMINATION (SEM-IV) 2016-17  
THEORY OF AUTOMATA AND FORMAL LANGUAGES**

Time : 3 Hours

Max. Marks : 100

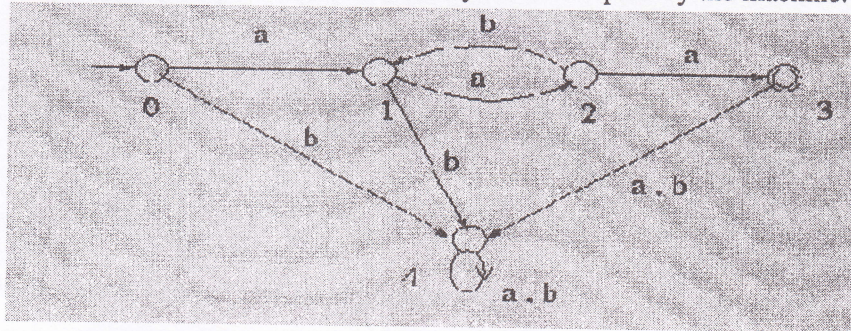
Note : Be precise in your answer. In case of numerical problem assume data wherever not provided.

**SECTION – A**

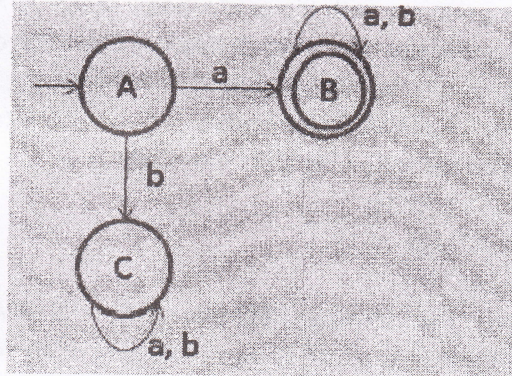
1. Explain the following:

10 x 2 = 20

- (a) Design the DFA that accepts an even number of a's and even number of b's.
- (b) Consider the DFA given below and identify the L accepted by the machine.



- (c) State the pumping lemma theorem for regular languages.
- (d) Convert the FA given below to left linear grammar.



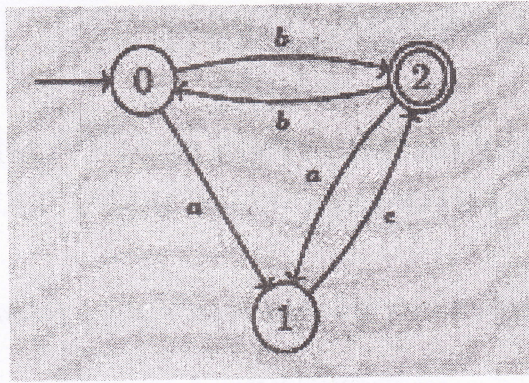
- (e) Check whether the grammar is ambiguous or not.  
 $R \rightarrow R+R / RR / R^* / a / b / c$ . Obtain the string  $w = a+b*c$
- (f)  $S \rightarrow aB/bA$   $A \rightarrow aS/bAA$   $B \rightarrow bS/aBB$ . Identify the strings obtained from this grammar.
- (g) Define PDA. Draw the graphical representation for PDA.
- (h) Design a PDA which accepts set of balanced parenthesis ( { { { } } } ).
- (i) Eliminate unit productions in the grammar.  $S \rightarrow A/bb$   $A \rightarrow B/b$   $B \rightarrow S/a$
- (j) What are checking off symbols?

**SECTION – B**

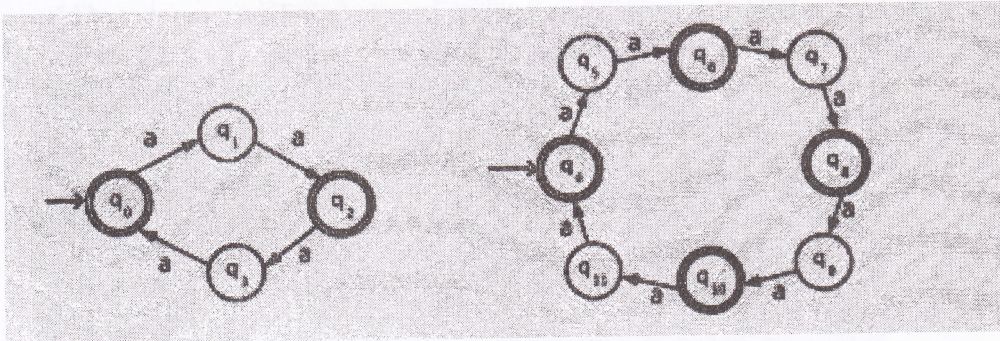
2. Attempt any five of the following questions:

5 x 10 = 50

- (a) (i) Convert the NFA-  $\epsilon$  to DFA.



(ii) Check with the comparison method for testing equivalence of two FA given below.



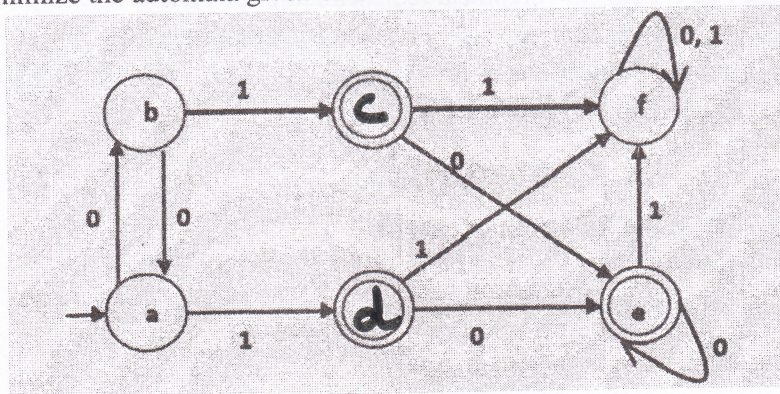
- (b) Prove that the compliment, homomorphism and inverse homomorphism, closure of a regular language is regular.
- (c) State and prove kleene's theorem with an example.
- (d) Consider the grammar with the production  $S \rightarrow aSS$   $A \rightarrow b$ . Compute the string  $aababbb$  with the left most and right most derivation. Draw the derivation tree.
- (e) (i) Find out whether the language  $L = \{x^n y^n z^n \mid n \geq 1\}$  is context free or not.  
(ii) Construct a PDA that accepts  $L = \{ww^R \mid w = (a+b)^*\}$
- (f) (i) Convert the following CFG into CNF  
 $S \rightarrow XY \mid Xn \mid p$   
 $X \rightarrow mX \mid m$   
 $Y \rightarrow Xn \mid o$   
 (ii) Convert the following CFG into CNF  $S \rightarrow ASA \mid aB, A \rightarrow B \mid S, B \rightarrow b \mid \epsilon$
- (g) Design a TM to recognize all strings consisting of an odd number of a's.
- (h) Prove that the halting problem is undecidable.

SECTION - C

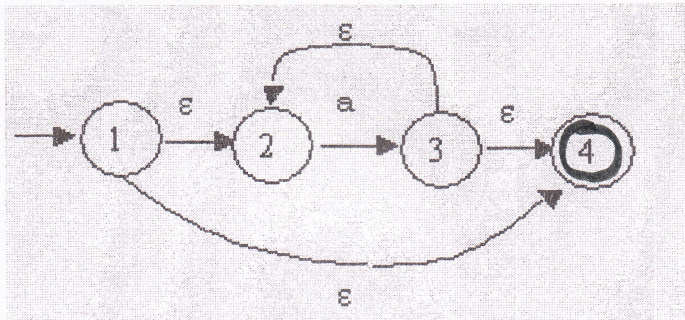
Attempt any two of the following questions:

2 x 15 = 30

3. (a) Minimize the automata given below



- (b) Compute the epsilon-closure for the given NFA. Convert it into DFA.



4. (a) Construct PDA to accept  $L = \{0^n 1^n \mid n \geq 0\}$   
(b) Construct a PDA from the following CFG.  
 $G = (\{S, X\}, \{a, b\}, P, S)$  where the productions are –  
 $S \rightarrow XS \mid \epsilon, A \rightarrow aXb \mid Ab \mid ab$
5. (a) Prove that single tape machines can simulate multi tape machines.  
(b) Design a TM to recognize all strings consisting of an odd number of  $\alpha$ 's.