

(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID : 2056

Roll No.

--	--	--	--	--	--	--	--	--	--

B.Tech.

(SEM. V) THEORY EXAMINATION 2010-11

## CONTROL SYSTEM

Time : 3 Hours

Total Marks : 100

Note : Attempt all questions. Each question carries equal marks.

1. Attempt any two parts of the following : (10×2=20)

- (a) Evaluate  $\frac{C}{R_1}$  and  $\frac{C}{R_2}$  for a system whose block diagram representation is shown in following Figure 1 (A) using block diagram reduction method.

representation is shown in following Figure 1 (A) using block diagram reduction method.

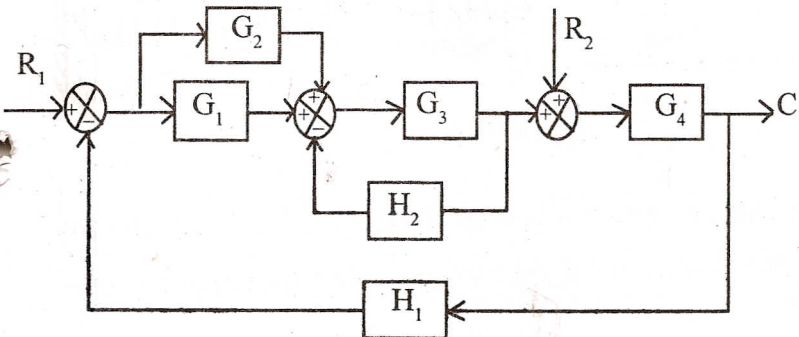


Figure 1 (A)

- (b) Obtain signal flow graph representation for a control system whose block diagram is given in the following Figure 1 (B). Find overall transfer function using Mason's gain formula.

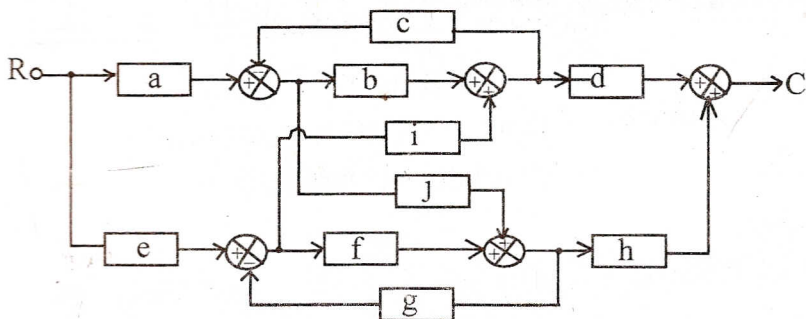


Figure 1 (B)

- (c) Find the transfer function  $X(s)/E(s)$  for the electromechanical system shown in following Figure 1 (C).

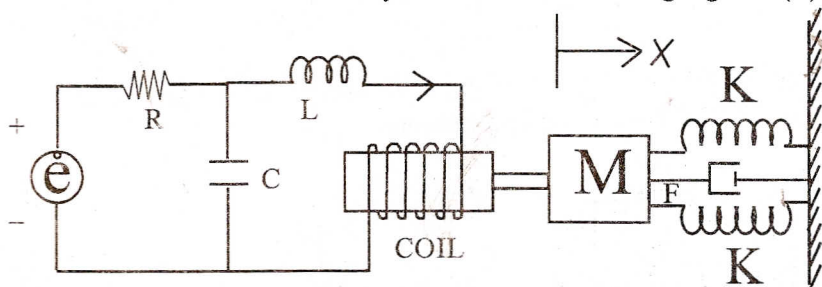


Figure 1 (C)

2. Attempt any **two** parts of the following : (10×2=20)

- (a) The overall transfer function of a control system is given by:

$$\frac{C(S)}{R(S)} = \frac{16}{S^2 + 1.5S + 16}$$

It is desired that the damping ratio is 0.8. Determine the derivative rate feedback constant  $K_1$  and compare rise time, peak time, maximum overshoot and steady state error for unit ramp input without and with derivative feedback control.

- (b) The maximum overshoot of a unity feedback control system having its forward path transfer function as  $G(S)=K/S(1+ST)$  is to be reduced from 60% to 20%. The system input is an unit step function. Determine the factor by which  $K$  should be reduced to achieve aforesaid reduction.
- (c) A control system is shown in following Fig. 2 (C)

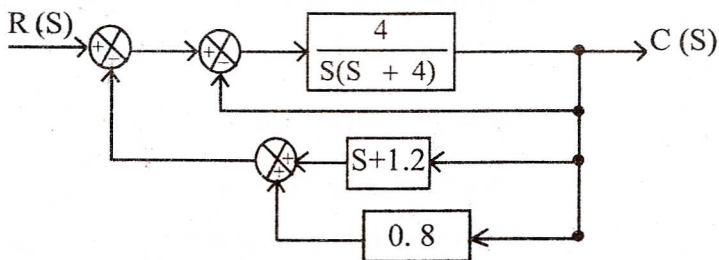


Figure 2 (C)

Determine the transfer function and derive an expression relating the output and time if the input is a step having a magnitude of 2 units.

3. Attempt any **two** parts of the following : (10×2=20)

- (a) The open loop transfer function of a control system is given by :

$$G(S)H(S) = \frac{K}{S(S+6)(S^2+4S+13)}$$

Sketch the root locus and explain the stability conditions of the control system.

- (b) (i) Using Routh-Hurwitz stability criterion, investigate the stability of a unity feedback control system whose open loop transfer function is given by :

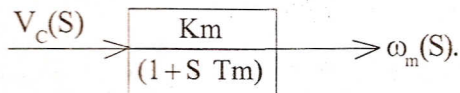
$$G(S) = e^{-ST}/S(S+2).$$

- (ii) The open loop transfer function of an unity feedback control system is given by :

$$G(S)H(S) = K/S(1+TS).$$

It is desired that all the roots of the characteristic equation must lie in the region to the left of the line  $S = -a$ . Determine the values of  $K$  and  $T$  required so that there are no roots to right of the line  $S = -a$ .

- (c) Prove that the simplified block diagram of an A.C. two phase servo motor relating  $\omega_m(S)$  and  $V_c(S)$  is given by :



4. Attempt any **two** parts of the following : (10×2=20)

- (a) Derive the transfer function of the control system from the data given on the Bode diagram as shown in the Fig. 4(A).

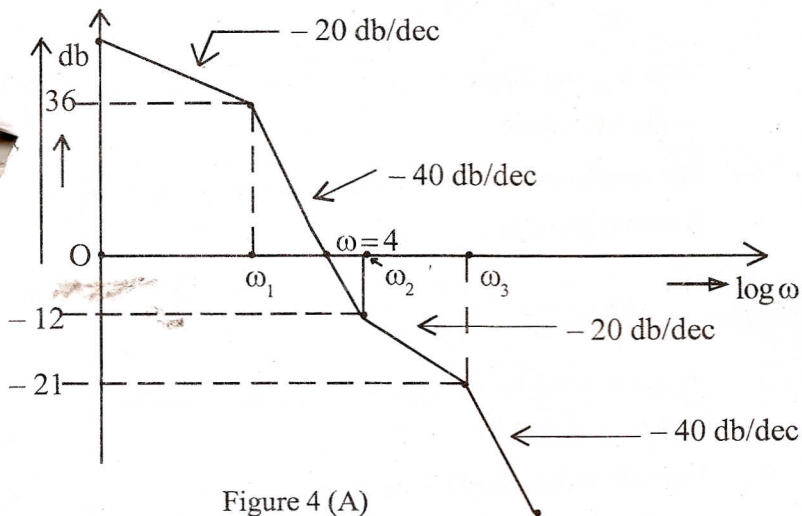


Figure 4 (A)

- (b) The open loop transfer function of a feed back control system is :

$$G(S) H(S) = \frac{K(1+2S)}{S(S+1)(S^2 + S+1)}$$

Find the restriction on K for stability using Nyquist stability criterion. Find the value of K for the system to have a gain margin of 3db. With this value of K. Find the phase cross over frequency and phase margin of the system.

- (c) The open loop transfer function  $G(j\omega)$  of a unity feed back control system is given by  $G(j\omega) = (x + jy)$ .

Draw constant Magnitude loci-M circles of the system.

Attempt any two parts of the following :

(10×2=20)

- (a) Construct the state model for a system characterised by the differential equation :

$$\frac{d^3 y}{dt^3} + 6 \frac{d^2 y}{dt^2} + 11 \frac{dy}{dt} + 6y = u.$$

Give the block diagram and signal flow graph representation of the state model.

- (b) The open loop transfer function of a unity feedback control system is given by :

$$G(S) = \frac{K}{S(1+0.2 S)}.$$

Design a suitable compensator such that the system will have  $K_v = 10$  and P.M. =  $50^\circ$ .

- (c) A system is described by the equations :

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} u.$$

$$y = [1 \quad 1 \quad 0]$$

Find if the system is completely observable. If not, find the mode which is not observable.