	. to be filled in your Answer Book)									
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B. Tech.

(SEM. V) THEORY EXAMINATION 2011-12

DESIGNANDANALYSIS OF ALGORITHMS

Time: 3 Hours

Total Marks: 100

Note: - Attempt all questions.

n elements in the worst case.

Attempt any four parts of the following: 1.

Ouick soit algorithm takes O (n2) time to soit

- (a) If $f(n) = a_m n^m + \dots + a_1 n + a_n$ and $a_m > 0$, then show that $f(n) = \Omega(n^m).$
- (b) Consider the following function: int RSUM(int A [], int n)

if (n) return RSUM (A, n-1) + A [n-1]; return 0; I - ni/2 and let n be the number of elements in

Determine the asymptotic complexity of the function

(c) Consider a polynomial

$$P(x) = (\dots (c_n * x + c_{n-1}) * x + c_{n-2}) * x + c_{n-3} * x \dots) * x + c_0.$$
 Estimate the time complexity to evaluate the polynomial

P(x).

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[Turn Over

- (d) Show that following equalities are incorrect:
 - (i) $n^2 \log n = \Theta(n^2)$
 - (ii) $n^2 / \log n = \Theta(n^2)$.
- (e) Sort the elements of the given array A using shell sort algorithm:

$$A = [20, 35, 18, 8, 14, 41, 3, 39]$$

- (f) Prove that Quick sort algorithm takes O (n²) time to sort an array of n elements in the worst case.
- 2. Attempt any two parts of the following:
 - (a) Define a red-black tree. Let h be the height of a red-black tree and let n be the number of internal nodes in the tree.

 Then show that:

$$h \le 2 \log_2(n+1)$$

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(b) Consider T is a B-tree of order m and height h. Letd = m/2 and let n be the number of elements in T. Then show that:

$$\log_{m} (n+1) \le h \le \log_{d} ((n+1)/2) +1.$$

(c) What is a Fibonacci heap? Discuss the applications of Fibonacci heaps.

- 3. Attempt any two parts of the following:
 - (a) Let T(n) = a T(n/b) + c, then show that $T(n) = O(\log n)$, if a = 1, otherwise $T(n) = O(n \log_b a)$.
 - (b) Give the high-level description of Kruskal's algorithm to find the minimum cost spanning tree of an n-vertex undirected network.
 - (c) What is an optimization problem? How are greedy method can be used to solve the optimization problem?
- 4. Attempt any **two** parts of the following:
 - (a) Explain dynamic programming method. Formulate dynamic programming recurrence equation for 0/1 knapsack problem.
 - (b) Describe travelling salesman problem (TSP). Show that a TSP can be solved using backtracking method in the exponential time.
 - (c) What is the graph coloring problem? What do you mean by optimal coloring of a graph? Show that every bipartite graph is 2-colorable.
- 5. Write short notes on any four parts of the following:
 - (a) NP completeness
 - (b) Approximation algorithms
 - (c) Fast Fourier transform
 - (d) String matching algorithms
 - (e) N-queen problem
 - (f) Hamiltonian cycles.