



(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID : 131602

Roll No.

### B. Tech.

(SEM. VI) THEORY EXAMINATION, 2014-15  
DIGITAL SIGNAL PROCESSING

Time : 3Hours]

[Total Marks : 100

1 Attempt any four parts 5×4=20

- (a) Draw the block diagram for the following system with input  $x(n)$  and output  $y(n)$

$$w(n) = x(n) + \frac{1}{2}x(n-1) \text{ and}$$

$$y(n) + \frac{1}{4}y(n-1) = w(n)$$

- (b) Obtain the cascade realization for the following system;

$$H(z) = \frac{(1 + \frac{3}{2}z^{-1} + \frac{1}{2}z^{-2})(1 - \frac{3}{2}z^{-1} + z^{-2})}{(1 + z^{-1} + \frac{1}{4}z^{-2})(1 + \frac{1}{4}z^{-1} + \frac{1}{2}z^{-2})}$$

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[ Contd...

- (c) Calculate the DFT of the sequence  $s(n)=\{2,4,2,3\}$ .
- (d) State and prove circular convolution property of DFT.
- (e) Explain frequency transformation with LPF to HPF conversion formula.
- (f) Draw a transformation matrix of size  $5 \times 5$  and explain the properties of twiddle factor.

2 Attempt any four parts 5×4=20

- (a) Determine  $H(z)$  using the impulse invariant technique for the analog system function

$$H(s) = \frac{1}{(s+0.5)(s^2+0.5s+2)}$$

- (b) Realise an FIR filter whose impulse response is  $h(n)=\{1, 2, 5, 6, 3, 6, 5, 2, 1\}$  using minimum number of multipliers.
- (c) Determine the response of a discrete-time system for an input signal  $s(n)=\{2,1, 3,1\}$ , if the unit-sample response is of the system is  $h(n)=\{1, 2,2,-1\}$
- (d) Enumerate and explain the properties of DFT.
- (e) Draw the parallel form network structure of the system with transfer function.

$$H(z) = \frac{2z(z+3)}{z^2+0.3z+0.02}$$

- (f) What are the different window functions used for windowing? Explain the effects of using different window functions for designing FIR filter on the filter response.

3 Attempt any two parts

10×2=20

- (a) Derive and draw the flow graph for DIF FFT algorithm for N=8.
- (b) Calculate the circular convolution of  $s_1(n) = \{1, 2, 1, 2\}$  and  $s_2(n) = \{1, 2, 3, 4\}$  using Stockham's method.
- (c) Determine  $H(z)$  for a butterworth filter satisfying the following constraints

$$\sqrt{0.5} \leq \begin{cases} |H(e^{j\omega})| \leq 1 & 0 \leq \omega \leq \frac{\pi}{2} \\ |H(e^{j\omega})| \leq 0.2 & \frac{3\pi}{4} \leq \omega \leq \pi \end{cases}$$

with  $T=1$  sec. Apply impulse invariant transformation

4 Attempt any two parts;

10×2=20

- (a) Given  $x(n) = 2^n$  and  $N=8$  find  $X(K)$  using DIT FFT algorithm. Also calculate the computational reduction factor.
- (b) Design a low-pass filter with the following desired frequency response

$$H_d(e^{j\omega}) = \begin{cases} e^{-j2\omega}, & -\frac{\pi}{4} \leq \omega \leq \frac{\pi}{4} \\ 0, & \frac{\pi}{4} < |\omega| < \pi \end{cases}$$

and using window function

$$w(n) = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{otherwise} \end{cases}$$



- (c) Draw the Ladder structure for the system with system function

$$H(z) = \frac{5z^{-3} + 2z^{-2} + 3z^{-1} + 1}{z^{-3} + z^{-2} + z^{-1} + 1}$$

5 Attempt any two parts : 10×2=20

- (a) Design a digital chebyshev filter to satisfy the constraints

$$0.77 \leq |H(e^{j\omega})| \leq 1 \quad 0 \leq \omega \leq 0.2\pi$$
$$|H(e^{j\omega})| \leq 0.1 \quad 0.5\pi \leq \omega \leq \pi$$

Using bilinear transformation with  $T=1s$

- (b) Convert the analog filter with system function

$$H(s) = \frac{s+0.1}{(s+0.1)^2 + 9} \text{ into digital filter with a}$$

resonant frequency of  $\omega_r = \frac{\pi}{4}$  of using bilinear transformation.

- (c) Explain the following phenomenon's :

- (i) Gibbs Oscillations.
- (ii) Frequency Wrapping.