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## BTECH

(SEM VI) THEORY EXAMINATION 2021-22 COMPUTER BASED NUMERICAL TECHNIQUES
Time: 3 Hours
Total Marks: 100
Note: Attempt all Sections. If you require any missing data, then choose suitably.

## SECTION A

1. Attempt all questions in brief.

$$
2 * 10=20
$$

| Q.no | Questions | Marks | CO |
| :--- | :--- | :--- | :--- |
| (a) | Define Rate of convergence of Bisection method | 2 | 1 |
| (b) | Add and Subtract the following floating point numbers: <br> $0.78596 \mathrm{E}-2$ and 0.78633E1 | 2 | 1 |
| (c) | Evaluate $\Delta^{\mathrm{n}}\left(\mathrm{e}^{3 \mathrm{x}+5}\right)$ | 2 | 2 |
| (d) | Write the relation between Divided differences and ordinary differences. | 2 | 2 |
| (e) | Write the formula of generalized Simpson's 1/3 Rule. | 2 | 3 |
| (f) | Find differentiation of Newton's forward difference formula | 2 | 3 |
| (g) | Define Predictor Corrector method. | 2 | 4 |
| (h) | Define Stability of solution. | 2 | 4 |
| (i) | Classify $u_{x x}+3 u_{x y}+u_{y y}=0$ | 2 | 5 |
| (j) | Define eigen vector of a matrix. | 2 | 5 |

## SECTION B

2. Attempt any three of the following:
$10 * 3=30$

| Q.no | Questions |  |  |  |  |  | $\mathrm{Ma}$ | CO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (a) | Using Regula Falsi Method find the real root of the equation $x^{3}-4 x-9=$ 0 upto 3 iteration. |  |  |  |  |  | 10 | 1 |
| (b) | Using Lagrange interpolation formula, calculate $f(3)$ from the following table:$\begin{array}{lrrrrrr} \mathrm{x}: & 0 & 1 & 2 & 4 & 5 & 6 \\ \mathrm{f}(\mathrm{x}): & 1 & 14 & 15 & 56 & 30 & 19 \\ \hline \end{array}$ |  |  |  |  |  | 10 | 2 |
| (c) | The velocity of a car which start initially from rest at interval of 2 minutes are given below |  |  |  |  |  | 10 | 3 |
|  | Time (minutes) | 2 | 4 | 6 | 10 | 12 |  |  |
|  | Velocity ( $\mathrm{Km} / \mathrm{hr}$ ) | 22 | 30 | 27 亿 18 | 7 | 0 |  |  |
|  | Apply Simpson's $3 / 8^{\text {th }}$ rule to find the distance covered by car |  |  |  |  |  |  |  |
| (d) | Find the value of $\mathrm{y}(1.1)$ using Runge-Kutta method of fourth order for the differential equation : $\frac{d y}{d x}=y^{2}+x y, y(1)=1.0$. Take $\mathrm{h}=0.05$ |  |  |  |  |  | 10 | 4 |
| (e) | Explain finite difference, method to the solution of Boundary value problemof second order. |  |  |  |  |  | 10 | 5 |

## SECTION C

3. Attempt any one part of the following:
$10 * 1=10$

| Q.no | Questions | Marks | CO |
| :--- | :--- | :--- | :--- |
| (a) | If $u=\frac{4 x^{2} y^{3}}{z^{4}}$ and errors in $x, y, z$ be 0.001, compute the relative maximum <br> error in $u$ when $x=y=z=1$ | 10 |  |
| (b) | Calculate $\sqrt{12}$ approximately using Newton-Raphson method. | 10 | 1 |

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4. Attempt any one part of the following
$10 * 1=10$

| Q.no | Questions |  |  | Marks |
| :--- | :--- | :--- | :--- | :--- |
| CO |  |  |  |  |
| (a) | Prove that $\Delta \log f(x)=\log \left[1+\frac{\Delta f(x)}{f(x)}\right]$ | 10 | 2 |  |
| (b) | Construct Newton forward interpolation polynomial for the datax 4 6 8 10 <br> y 1 3 8 16 <br> Hence evaluated y for $\mathrm{x}=5$.     | 10 | 2 |  |

5. Attempt any one part of the following:
$10 * 1=10$

| Q.no | Questions | Marks | CO |
| :---: | :---: | :---: | :---: |
| (a) | Compute $\mathrm{f}^{\prime}(\mathrm{x})$ at $\mathrm{x}=16$ from the given data    <br> $\mathrm{x}:$ 15 17 19 21 <br> $\mathrm{f}(\mathrm{x})=\sqrt{x}:$ 3.87 4.12 4.35 4.58 | 10 | 3 |
| (b) | Find the value of the integral using trapezoidal rule, taking $\mathrm{h}=0.25$ $\int_{0}^{1} \frac{d x}{1+x^{2}}$ | 10 | 3 |

6. Attempt any one part of the following:

$$
10 * 1=10
$$

| Q.no | Questions | Marks | CO |
| :--- | :--- | :--- | :--- |
| (a) | Use Picard's method; obtain the solution of the equation <br> $\frac{d y}{d x}=x\left(1+x^{3} y\right), y(0)=3$. | 10 <br> Compute the value of $y(.1) a n d y(.2)$ | 4 |
| (b) | Write the algorithm of Euler's method to the solution of ordinary differential <br> equation. | 10 | 4 |

7. Attempt any one part of the following:

10*1 = 10

| Q.no | Questions | Marks | CO |
| :--- | :--- | :--- | :--- |
| (a) | Explain Explicit method to solve parabolic one dimensional Heat equation | 10 | 5 |
| (b) | Using Power method, find Eigen values and Eigen vector of A | 10 | 5 |
|  | $\mathrm{~A}=\left[\begin{array}{cr}4 & 1 \\ -1 & 6\end{array}\right]$ |  |  |

