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M.C.A.
(SEM I) THEORY EXAMINATION 2017-18
DISCRETE MATHEMATICS

Time: 3 Hours

Total Marks: 70

- Note:** 1. Attempt all Sections. If require any missing data; then choose suitably.
 2. Any special paper specific instruction.

SECTION A

1. Attempt *all* questions in brief.

2 x 7 = 14

- a. What do you mean by power set? Illustrate with an example.
- b. Let f and $g: \mathbb{R} \rightarrow \mathbb{R}$, be defined as follows:
 $f(x) = x + 2$, $g(x) = 1 / (x^2 + 1)$. Compute $f \circ g(x)$
- c. State and prove De Morgan's law for logic.
- d. What do you mean by equivalence relations?
- e. Draw the hasse diagram of poset $(D_{72}, '|')$. $'|'$ represent the divisibility operation.
- f. Write and prove 'Modus Ponens' rule of inference.
- g. Let $A = \{1, 2, 3, 4, 5, 6\}$. Compute $(4, 1, 3, 5) \circ (5, 6, 3)$.

SECTION B

2. Attempt any *three* of the following:

7 x 3 = 21

- a. Show that for any two sets, A and B:
 $A - (A \cap B) = A - B$.
 Also draw Venn diagrams for both.
- b. Define linearly orders set and partially ordered set. Explain the properties, a poset must satisfy?
- c. Using mathematical induction, show that $11^{n+1} + 122^{n-1}$ is divisible by 133 for all $n \geq 1$.
- d. Solve the following recurrence relations:
 (i) $f_n = 5f_{n-1} + 6f_{n-2}$
 (ii) $d_n = 2d_{n-1} - d_{n-2}$
- e. Prove the validity of the following argument without using truth table:
 "If I get the job and work hard, then I will get promoted. If I get promoted, then I will be happy. I will not be happy. Therefore, either I will not get the job or I will not work hard"

SECTION C

3. Attempt any *one* part of the following:

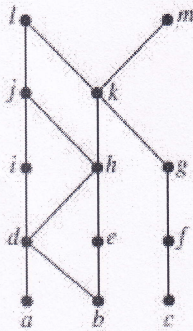
7 x 1 = 7

- (a) Prove that the relation "Congruence Modulo m ", given by $'\Xi' = \{ (x, y) \mid x - y \text{ is divisible by } m \}$, over the set of positive integers is an equivalence relation.
 Also, show that if $x_1 \Xi y_1$ and $x_2 \Xi y_2$, then $(x_1 + x_2) \Xi (y_1 + y_2)$
- (b) What do you mean by function? Explain different types of functions with proper examples.

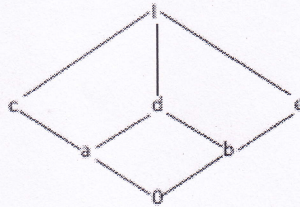
4. Attempt any *one* part of the following:

7 x 1 = 7

- (a) Define Supremum and infimum for a partial order. Determine LUB and GLB of following subsets for Hasse diagram given below:
 (i) $\{a, b, c\}$
 (ii) $\{f, g, h\}$



- (b) What do you mean by distributed lattice and complemented lattice? Consider the bounded lattice L , given below. Check whether it is distributive or not.



5. Attempt any *one* part of the following:

7 x 1 = 7

- (a) Use a K-map to find a minimal sum for:
 $E = y't' + y'z't + x'y'zt + yzt'$
 Also draw the circuit diagram for the expression obtained.
- (b) Define minterms and maxterms with examples. Express the Boolean function $f(x, y, z) = x + y'z$ as a sum of minterms.

6. Attempt any *one* part of the following:

7 x 1 = 7

- (a) Write the following conditional statement in symbolic form. Also give the converse, inverse and contra-positive of the statement:
 "If the flood destroys Mohan's house or the fire destroy Mohan's house, then Mohan's insurance company will pay him."
- (b) What do you mean by existential quantifiers and universal quantifiers? Explain with proper examples.
 Find a counterexample, if possible, to these universally quantified statements, where the domain for all variables consists of all integers.

- (i) $\forall x(x^2 \geq x)$
 (ii) $\forall x(x > 0 \vee x < 0)$
 (iii) $\forall x(x = 1)$

7. Attempt any *one* part of the following:

7 x 1 = 7

- (a) Solve the following linear nonhomogeneous recurrence relation with constant coefficient:
 $a_n = 5a_{n-1} + 6a_{n-2} + 3.5^n$ where $a_0 = 4$ and $a_1 = 7$
 Verify your answer for a_2 .
- (b) Write short notes on following:
 (i) Poyla's Counting Theorem
 (ii) Pigeonhole Principle